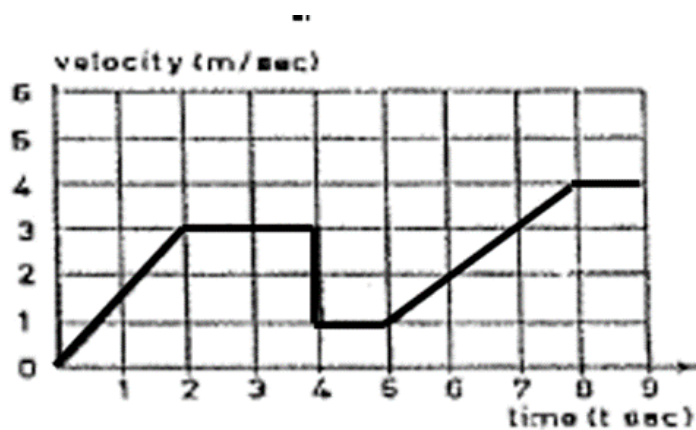


## Momentum and impulse



The above graph represents a plot of velocity against time of a cart of initial mass 1 kg as it travels in a straight line across a level surface. At some instant during the 9 seconds, an additional mass was dropped vertically on to the cart.

### 1967 Question 15, 1 mark

At what time did this occur?

### 1967 Question 16, 1 mark

What was the value (in kg) of the additional mass dropped vertically on to the cart?

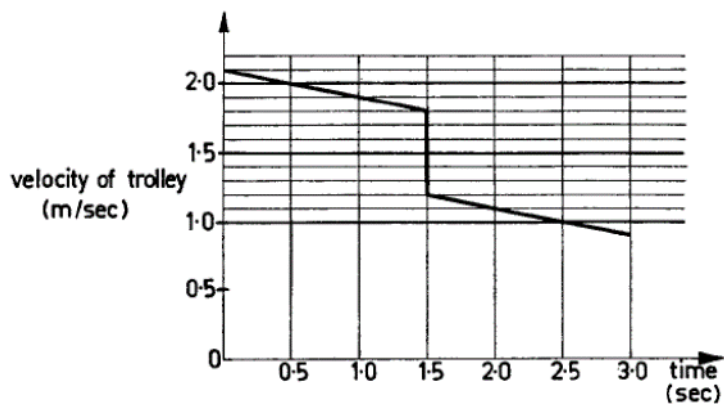
A meteor assumed to be of constant mass 1 kg, moving with a speed  $12,000 \text{ m s}^{-1}$ , is travelling vertically down towards a planet. The planet's dense atmosphere slows it down to  $10,000 \text{ m s}^{-1}$  in 4 secs.

### 1969 Question 10, 2 marks (modified)

At the end of this 4 seconds when the meteor has slowed to  $10,000 \text{ m s}^{-1}$ , the meteor strikes a space vehicle of mass 200 kg which is moving horizontally at a speed of  $10,000 \text{ m s}^{-1}$ . The collision takes place in such a way that the meteor lodges in the space vehicle. What is the tangent of the angle  $\theta$  to the horizontal with which the vehicle continues its course immediately after the collision and what is its speed?

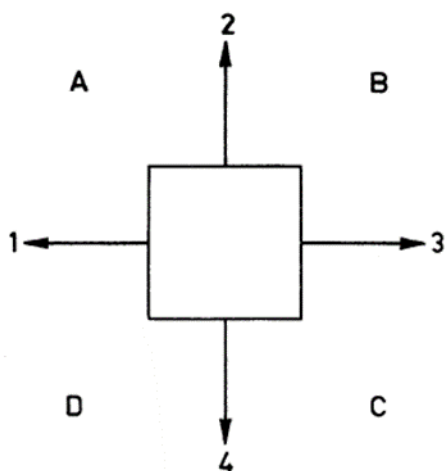
## Momentum and impulse

A trolley of mass 6.0 kilogram is given a push and then allowed to roll freely along a table. Its velocity is measured continuously. At time 1.5 second a lump of clay is dropped vertically onto the trolley



### 1970 Question 14, 1 mark

What was the mass of the lump of clay which was dropped onto the trolley?



A sled resting on a smooth horizontal ice surface is equipped with four identical fixed catapults. Each catapult throws a 1.0 kg projectile horizontally at a speed of  $100 \text{ m s}^{-1}$  relative to the sled. The total mass of the sled and projectiles before firing is 10 kg.

The catapults are fired in order 1, 2, 3, 4 in the directions shown.

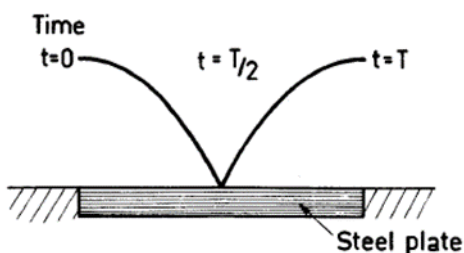
### 1971 Question 7, 1 mark

What is the speed of the sled relative to the ice after the first catapult is fired?

**1971 Question 8, 1 mark**

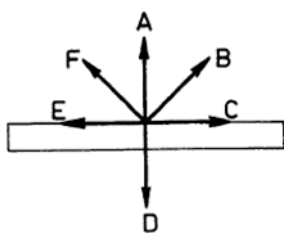
State the quadrant (A, B, C or D) into which the final velocity of the sled is directed after all the catapults are fired, if the final velocity is zero give E as your answer.

A steel ball is projected horizontally and makes a perfectly elastic collision with a steel plate embedded in the ground.



**1971 Question 38, 1 mark**

Which arrow (A - F) best describes the direction of the impulse of the plate on the ball?



**1971 Question 39, 1 mark**

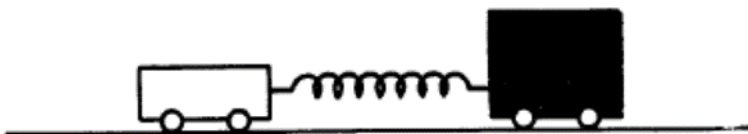
Which one or more of the following statements about the momentum of the ball are true?

- A. The horizontal component of the momentum of the ball remains constant throughout the time interval  $0 \leq t \leq T$
- B. The vertical component of the momentum just before  $t = \frac{T}{2}$  is equal to the vertical component just after  $t = \frac{T}{2}$  because the collision is elastic.

Momentum and impulse

- C. The total momentum of the ball remains constant throughout the time interval  $0 \leq t \leq T$ , but the horizontal component is partly changed into a vertical component due to the action of the gravitational field.
- D. During the impact there is a transfer of momentum to the earth.

(one or more answers)



A light spring is permanently connected between two trolleys of masses, 1.0 kg and 4.0 kg which can move along a straight horizontal track. The spring is compressed and then the trolleys are released simultaneously from rest.

**1971 Question 40, 1 mark**

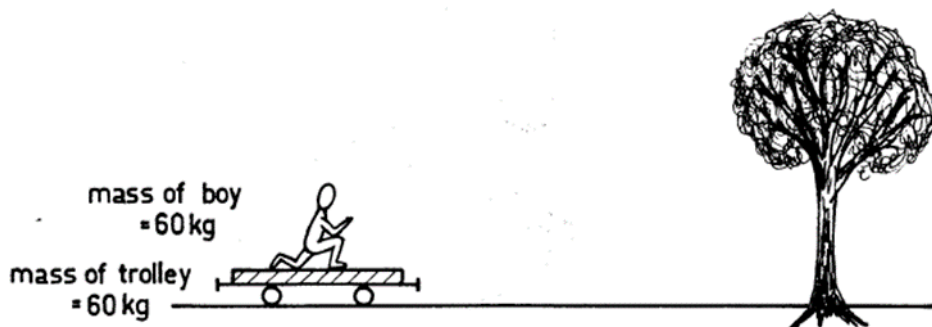
What is the speed of the lighter trolley when the speed of the heavier trolley is  $2 \text{ m sec}^{-1}$ ?

**1971 Question 42, 1 mark**

When the heavier trolley first comes momentarily to rest, the velocity of the lighter trolley is

- A. zero.
- B. in the same direction as its initial velocity.
- C. in the opposite direction to its initial velocity.
- D. indeterminate - there is not enough information given.

A boy of mass 60 kg rides on a 60 kg trolley moving with constant speed of  $5 \text{ m s}^{-1}$  along a horizontal track. Frictional forces can be neglected. The boy jumps vertically with respect to the moving trolley to grab the overhanging branch of a tree.



**1972 Question 23, 1 mark**

## Momentum and impulse

What is the speed of the trolley after the boy has jumped off?

A trolley of mass 100 kg moving with velocity  $6.0 \text{ m s}^{-1}$  collides with a stationary trolley of mass 50 kg, and becomes coupled to it.

### 1972 Question 37, 1 mark

How much kinetic energy is lost in the collision?

### 1972 Question 39, 1 mark

The area under the graph of **net force** versus **time** for an object represents

- A change in potential energy
- B acceleration
- C work done
- D power
- E change in momentum

The following data were obtained from a multi-flash photograph of a golf club hitting a stationary ball.

Speed of club head just before impact  $50 \text{ m s}^{-1}$

Speed of club head just after impact  $32 \text{ m s}^{-1}$

The mass of the golf ball is 0.050 kg.

The effective mass of the golf club (which may be assumed to be concentrated in the head) is 0.20 kg.

**Include units in answers to questions 28, 29, and 31.**

### 1973 Question 28, 1 mark

What is the impulse on the ball?

## Momentum and impulse

### 1973 Question 29, 1 mark

The club and ball are in contact for 0.010s. What is the average force exerted on the ball?

### 1973 Question 30, 1 mark

What is the initial velocity of the ball?

### 1973 Question 31, 1 mark

How much kinetic energy is lost in the impact?

A sphere of mass 3 kg travelling North at  $2 \text{ m s}^{-1}$  collides with another sphere of mass 4 kg travelling East at  $2 \text{ m s}^{-1}$ .

### 1975 Question 8, 1 mark

The magnitude of their resultant momentum after collision will be:

- A zero
- B  $2 \text{ kg m s}^{-1}$
- C  $10 \text{ kg m s}^{-1}$
- D  $14 \text{ kg m s}^{-1}$
- E dependent on whether the collision was elastic or inelastic

Momentum and impulse

**1975 Question 9, 1 mark**

The total kinetic energy of the two spheres after collision will be:

- A 10 J
- B 14 J
- C 20 J
- D 28 J
- E dependent on whether the collision was elastic or inelastic

An object of mass 4.0 kg, has an initial velocity of 2.0 m s<sup>-1</sup> north and a final velocity of 3.0 m s<sup>-1</sup> south.

**1976 Question 12, 1 mark**

What is the magnitude of the change in momentum?

Various physical quantities can often be calculated from the area under graphs relating two physical quantities. For example, displacement can be found by calculating the area under a velocity versus time graph.

**1976 Question 18, 1 mark**

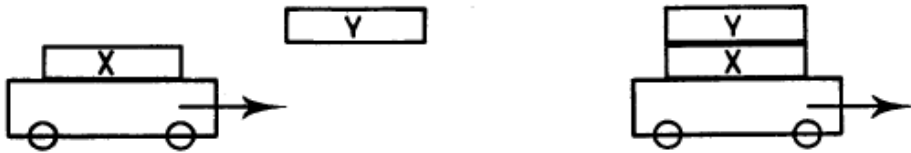
The area under a graph of net force versus time for an object represents

- A. change in Potential energy.
- B. acceleration.
- C. work done.
- D. power.
- E. change in momentum.

In an experiment, a laboratory cart carrying one brick is travelling at constant speed along a smooth level bench. Another identical brick is dropped at time T on to the cart.

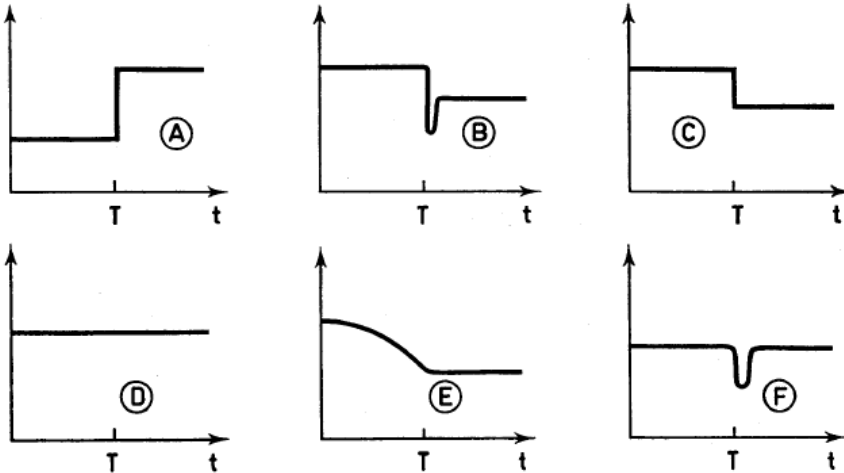
The mass of the cart is equal to the mass of 1.5 bricks.

Momentum and impulse



1976 Question 21, 1 mark

Which of the graphs (A - F) below best represents the velocity of the cart as a function of time?



1976 Question 23, 1 mark

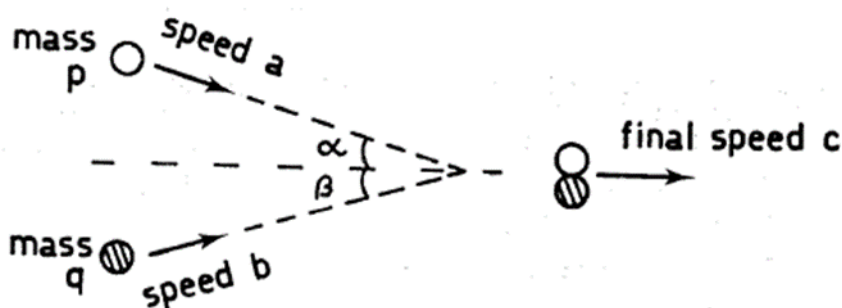
Which of the graphs (A - F) above best represents the momentum of brick X?

1976 Question 24, 1 mark

Which of the graphs (A - F) above best represents the total energy of cart and bricks?

1976 Question 25, 1 mark

In a second experiment, the same cart carries three identical bricks and is travelling at a constant speed of  $1.1 \text{ ms}^{-1}$ .  
 1. A fourth brick is dropped on to the cart. What will the speed of the cart now be?





## Momentum and impulse

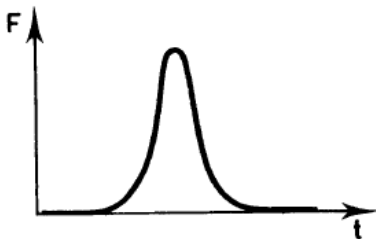
Two masses  $p$  and  $q$  collide, stick together, and move off as shown in the figure.

### 1977 Question 25, 1 mark

Which *two* of the following equations correctly describe the motions of these masses?

- A.  $pa + qb = (p + q)c.$                       B.  $pa^2 + qb^2 = (p + q)c^2.$   
C.  $pa \cos\alpha + qb \cos\beta = (p + q)c.$                       D.  $pa^2 \cos^2\alpha + qb' \cos^2 \beta = (p + q) c^2.$   
E.  $pa \sin\alpha + qb \sin\beta = (p + q)c.$                       F.  $pa \sin\alpha - qb \sin\beta = 0.$   
G.  $pa^2 \sin^2\alpha - qb^2 \sin^2\beta = 0.$

A cricket ball, travelling horizontally, is hit by a batsman so that it quickly returns to the bowler. The graph represents the variation of the force of the bat on the ball with time.



### 1978 Question 9, 1 mark

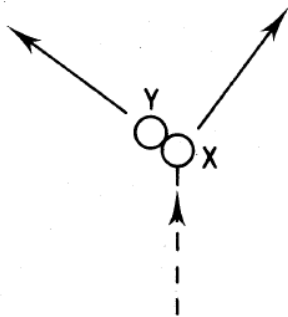
The area under this graph represents:

- A. The impulse of the bat on the ball  
B. The change in kinetic energy of the ball  
C. The change in momentum of the ball  
D. The average force on the ball during the time of contact  
E. The work done on the ball.

(one or more answers)

During a game of billiards, ball X strikes the stationary ball Y so that X and Y follow the paths shown.

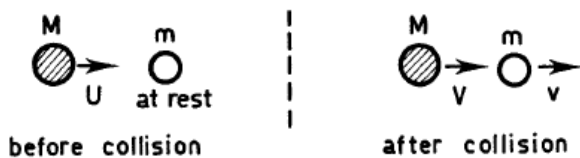
Momentum and impulse



1978 Question 22, 1 mark

Which of the following statements about the momentum of ball X is correct?

- A. Neither the magnitude nor the direction of the momentum has changed.
- B. Only the direction of the momentum has changed.
- C. The magnitude of the momentum has increased.
- D. The magnitude of the momentum has decreased.



A ball of mass  $M$  strikes a stationary ball of mass  $m$  elastically, and head-on.

1979 Question 24, 1 mark

Which two of the following equations are correct?

- A.  $U = v + V$
- B.  $MU^2 = mv^2 + MV^2$
- C.  $M^2U^2 = m^2v^2 + M^2V^2$
- D.  $MU = (m + M)(v + V)$
- E.  $MU = mv + MV$ .

(one or more answers)

1979 Question 25, 1 mark

If the balls are of equal mass, i.e.  $\frac{M}{m} = 1$ , then,

Momentum and impulse

- A.  $V = \frac{1}{2} U$  and  $v = \frac{1}{2} U$
- B.  $V = 0$  and  $v = U$
- C.  $V = U$  and  $v = 0$
- D.  $V = -U$  and  $v = 2U$
- E.  $V = -\frac{1}{2}U$  and  $v = \frac{1}{2}U$

1979 Question 26, 1 mark

If the balls are of unequal mass, then the ratio  $\frac{V}{v}$  is equal to

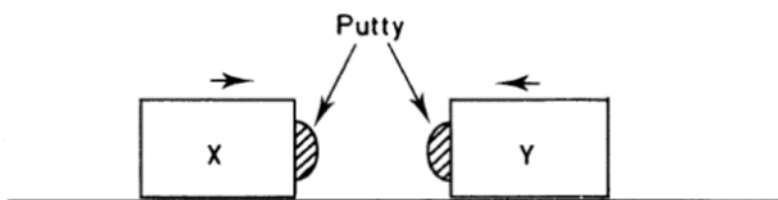
- A.  $\frac{M-m}{2M}$
- B.  $\frac{M-m}{2m}$
- C.  $\frac{m}{M}$
- D.  $\frac{M}{M-m}$
- E.  $\frac{m}{M+m}$

1979 Question 27, 1 mark

If, instead of colliding elastically, the two masses had stuck together and moved off with velocity  $W$ , which of the following statements would be correct?

- A.  $MU = (M + m)W$ .
- B.  $\frac{1}{2} MU^2 = \frac{1}{2} (M + m)W^2$
- C.  $M^2U^2 = M^2W^2 + m^2W^2$ .
- D. More than one of the above equations are correct.
- E. None of the above equations is correct.

Momentum and impulse

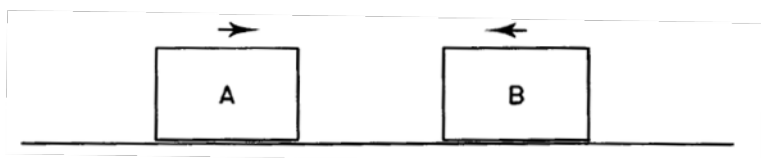


Two identical blocks, **X** and **Y**, are moving towards each other on a frictionless surface, with equal speeds. A piece of putty on the end of each block results in their sticking together on contact.

**1980 Question 30, 1 mark**

What has happened to the total momentum of the two blocks as a result of the interaction?

- A. All the momentum has been lost; the collision is inelastic, so the momentum is dissipated as heat.
- B. It has been transferred to the earth.
- C. It is now stored in the molecules of the blocks and the putty.
- D. Nothing has happened: it remains zero.

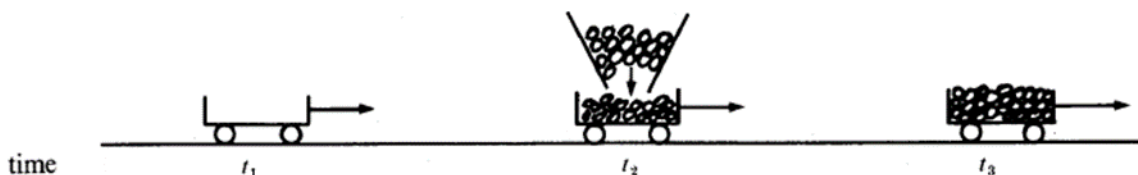


**1980 Question 31, 1 mark**

Another pair of identical pucks, **A** and **B**, move towards each other on a frictionless surface with equal speeds. The pucks move apart after colliding.

During the interaction,  $\frac{3}{4}$  of the total kinetic energy that the two pucks had before the collision is lost.

What is the value of the ratio  $\frac{\text{magnitude of momentum of A before the collision}}{\text{magnitude of momentum of A after the collision}}$



An empty railway truck of mass  $M$  travels at constant speed  $v$  under a coal chute. At time  $t_2$ , a load of coal of mass  $m$  is dropped vertically into the truck.

**1981 Question 27, 1 mark**

What is the speed of the truck immediately afterwards?

**1981 Question 28, 1 mark**

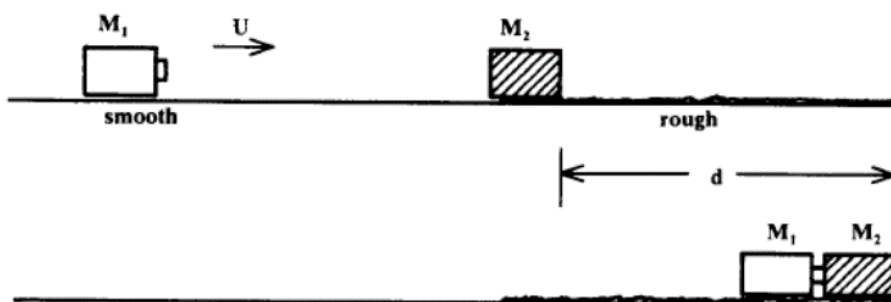
The gain in horizontal momentum of the coal is due to:

- A. the impulse given to the coal by the truck.
- B. the conversion of vertical kinetic energy into horizontal kinetic energy.
- C. the force of gravity acting on the coal as it falls into the truck.
- D. the conversion of potential energy into kinetic energy.

**1981 Question 29, 1 mark**

The falling coal had vertical momentum as it landed on the truck. What happened to this momentum?

- A. It was transferred to the earth.
- B. It was converted into horizontal momentum by the force of the walls of the truck on the coal.
- C. It was lost as heat and sound as the coal came to rest relative to the truck.
- D. It is stored in the coal in the form of potential energy'



A block of wood, with a piece of putty attached (total mass  $M_1$ ) is travelling at a constant speed  $U$  over a frictionless surface. It strikes a second block ( $M_2$ ) and the two move off together with an initial velocity  $V$  and initial kinetic energy  $K$ . The blocks are subjected to a constant frictional force  $F$ , and come to rest after travelling a distance  $d$ .

**1982 Question 11, 1 mark**

Write an expression for  $V$  in terms of  $M_1$ ,  $M_2$  and  $U$ .

## Momentum and impulse

### 1982 Question 12, 1 mark

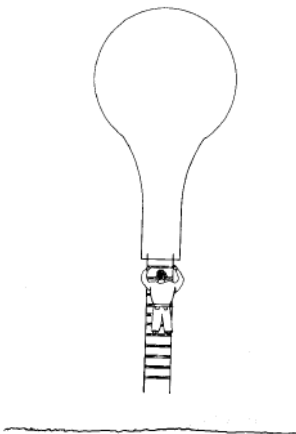
Which of the following statements about the total momentum of the blocks is correct?

- A. Some of it is lost during the impact because the collision is inelastic; after that no momentum is lost, only kinetic energy.
- B. Some of it is transferred (without loss) from  $M_1$  to  $M_2$  during the impact; the frictional force then causes the blocks to transfer momentum to the earth.
- C. Some of it is lost during the impact, and the remainder is lost as the blocks travel along the rough surface.
- D. The total momentum of the two masses remains the same.

### 1982 Question 21, 1 mark

An ice skater of mass 60 kg travelling **north** at  $5 \text{ m s}^{-1}$ , is carrying a parcel of mass 10 kg. The skater drops the parcel to the floor. What is the velocity of the skater now (magnitude and direction)?

A man of mass  $m$  is standing on a rope ladder suspended below a free-floating balloon. The mass of the balloon and ladder is  $M$ . The balloon is stationary relative to the ground.



The man now climbs up the ladder at a speed  $v$  relative to the ground.

### 1983 Question 21, 1 mark

Momentum and impulse

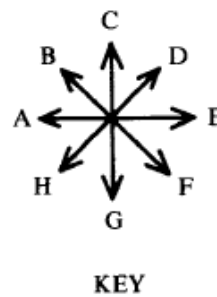
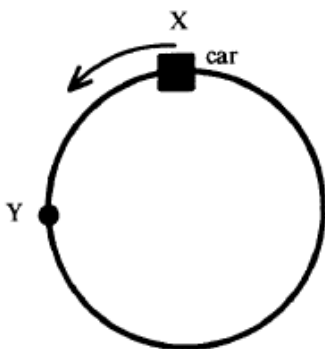
With what speed relative to the ground does the balloon move, if at all?

**1983 Question 22, 1 mark**

The man now stops climbing.

With what speed relative to the ground does the balloon now move?

The diagram below represents a car of mass 1000 kg travelling anticlockwise around a horizontal circular track of radius 200 m at a constant speed of  $20 \text{ m s}^{-1}$ .



Use the key to answer the next two questions.

**1983 Question 24, 1 mark**

What is the direction of the car's momentum when it is at position X?

**1983 Question 25, 1 mark**

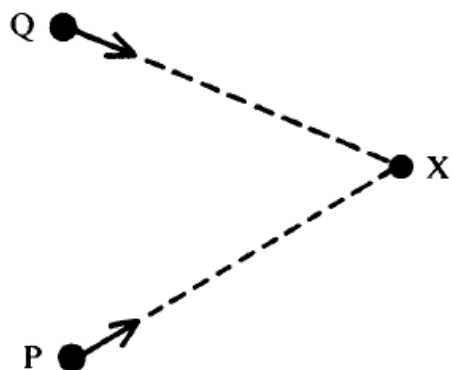
What is the direction of the change in momentum of the car when it moves from position X to position Y?

**1983 Question 26, 1 mark**

What is the magnitude of the change in momentum of the car when it moves from position X to position Y?

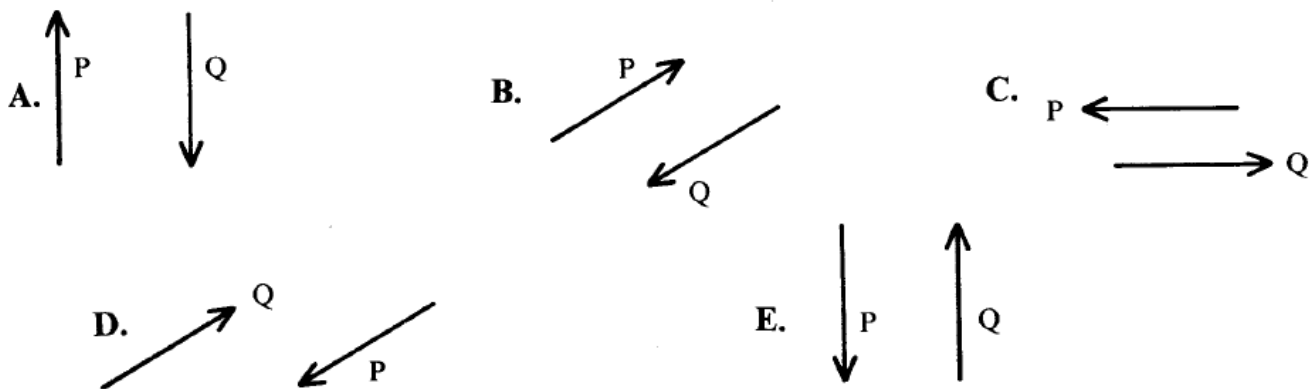
Momentum and impulse

Consider the following collision (shown below) between two identical ball-bearings (P and Q) travelling at the same speed and moving in the directions shown.



1984 Question 21, 1 mark

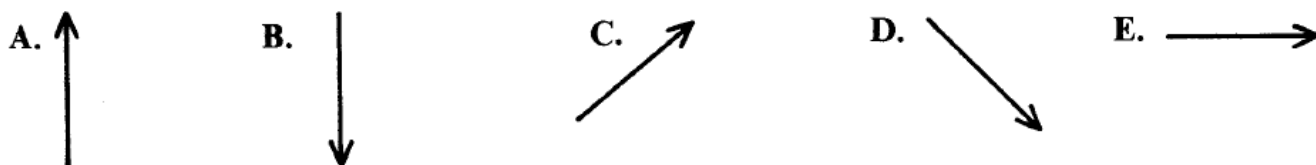
Assuming that the ball-bearings undergo an elastic collision at the point X, in which of the following diagrams do the arrows represent the change in momentum of each ball-bearing P and Q?



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1984 Question 22, 1 mark

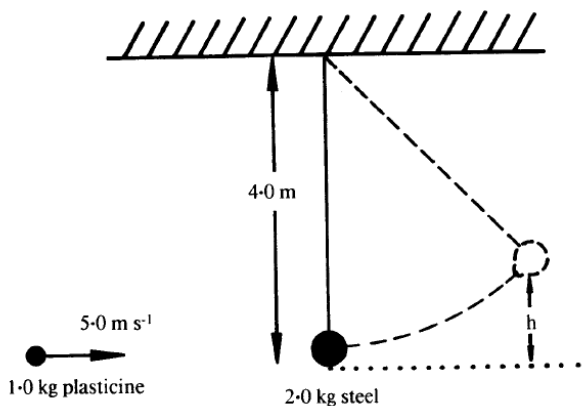
Which of the arrows below best represents the **impulse** applied to ball-bearing P by Q during the collision?





## Momentum and impulse

A 2.0 kg steel ball is hanging on a light inextensible string which is attached to a solid support. A 1.0 kg ball of plasticine is thrown with a horizontal velocity of  $5.0 \text{ m s}^{-1}$  at the hanging ball. It collides head-on with the hanging ball and sticks to it. In the following two questions take the acceleration due to gravity,  $g$  to be  $10 \text{ m s}^{-2}$ .



### 1984 Question 30, 1 mark

What is the momentum of the two balls immediately after the collision?

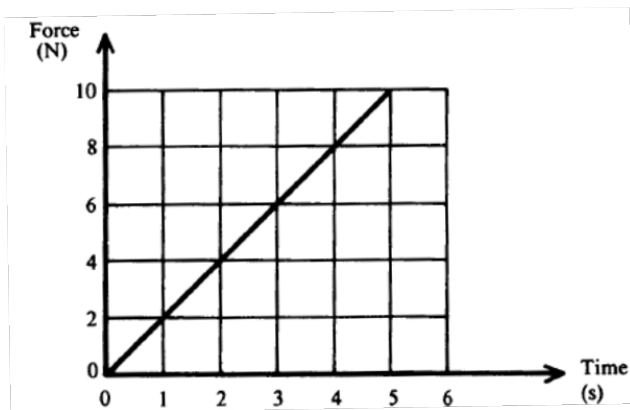
### 1984 Question 32, 1 mark

At the top of its motion the mass has no momentum. Which of the statements below best explains this situation?

- A. Momentum is not conserved in inelastic collisions.
- B. The momentum has been converted to potential energy.
- C. The momentum is stored as the tension in the string.
- D. The momentum has been transferred to the earth via the support.
- E. The momentum was dissipated as heat and sound during the collision.

A body of mass  $2.0 \text{ kg}$  moves from rest, in a straight line, under the action of a net force that increases with time as shown in the graph below.

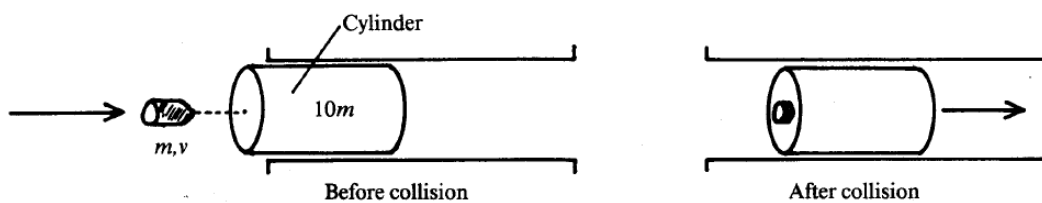
## Momentum and impulse



### 1985 Question 12, 1 mark

What is the change in momentum of the body in the first 5.0 s?

A bullet of mass  $m$  and velocity  $v$  is fired directly at a solid cylinder of mass  $10m$ , which can slide smoothly inside a horizontal tube as shown.



When the bullet hits, it sticks to the front of the cylinder, and the total mass slides forward as shown.

Answers to Questions 5 to 8 should be expressed in terms of  $m$  and  $v$ .

### 1986 Question 5, 1 mark

What is the velocity of the bullet-cylinder system after the collision?

### 1986 Question 7, 1 mark

What impulse did the bullet give to the cylinder?

### 1986 Question 8, 1 mark

If the collision occurred over a time interval  $T$ , what average force acted on the cylinder during the collision?

## Momentum and impulse

A person of mass 60 kg is held in the back seat of a car by a seat-belt. The belt is attached firmly to the body of the car.

The car, which is travelling at a speed of  $25 \text{ m s}^{-1}$  collides with a tree, and stops. The passenger, still restrained by the seat-belt, stops moving 0.15 s after the initial impact.

### 1987 Question 28, 1 mark

What is the magnitude of the impulse given to the passenger by the seat-belt?

### 1987 Question 29, 1 mark

What is the average force exerted on the person by the seat-belt?

### 1987 Question 30, 1 mark

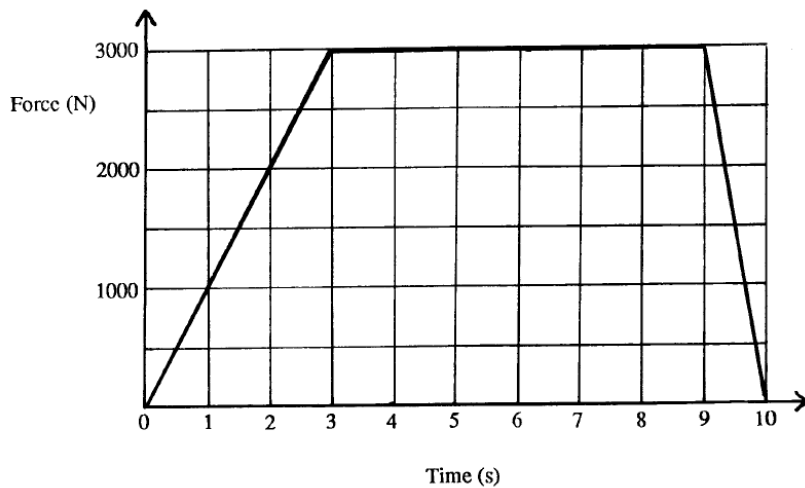
After the collision, the passenger has no momentum. Which of the statements ( A- D) below best describes what happened to the momentum that the passenger had originally?

- A. It has been dissipated as heat and sound.
- B. It has been stored as potential energy in the seat-belt which has stretched.
- C. It has been transferred to the car and hence to the earth.
- D. It has been recovered by the passenger, who recoils backward after the car stops.

A physicist is carrying out a study into the distance required for a car of mass 1000 kg to brake to a stop under various conditions. One test was carried out on a straight, level road.

The figure below shows the resultant force on the car as a function of time from the instant the brakes were applied ( $t = 0 \text{ s}$ ). The car came to a stop after 10.0 s.

## Momentum and impulse



### 1988 Question 4, 1 mark

What was the magnitude of the change in momentum of the car in the 10.0 seconds?

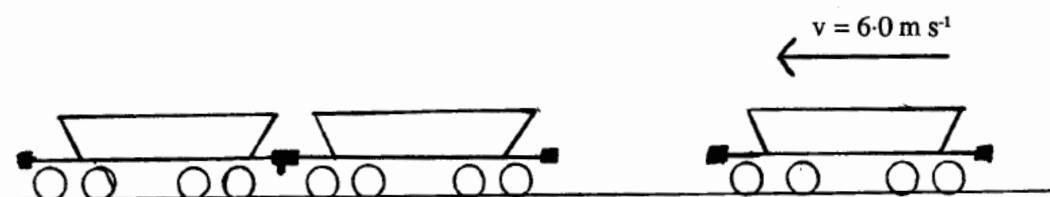
### 1988 Question 5, 1 mark

What was the initial speed of the car at  $t = 0$  s?

During shunting, a railway truck is moving at  $6.0 \text{ m s}^{-1}$  towards two stationary trucks which are coupled together. This is shown in below.

Each of the trucks has a mass of  $3.0 \times 10^4 \text{ kg}$ .

(Ignore any friction forces.)



The trucks collide and couple together.

### 1988 Question 16, 1 mark

What is the speed of the trucks after the collision?

### 1988 Question 17, 1 mark

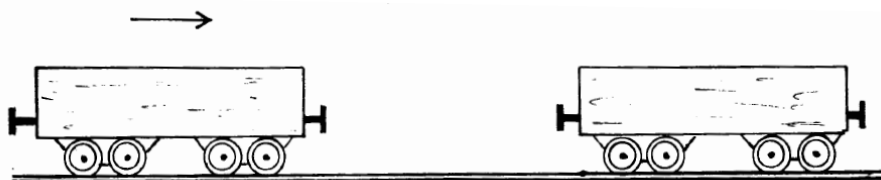
## Momentum and impulse

Which of the statements (A - D) below is true for this collision?

- A. Momentum and kinetic energy are conserved.
- B. Neither momentum nor kinetic energy is conserved.
- C. Kinetic energy is conserved but momentum is not conserved.
- D. Momentum is conserved but kinetic energy is not conserved.

During shunting, a railway truck is moving with a constant velocity of  $3.0 \text{ m s}^{-1}$  towards a stationary truck as shown below.

Each truck has a mass of  $2.0 \times 10^4 \text{ kg}$ . Ignore any friction forces.



The two trucks collide and couple together.

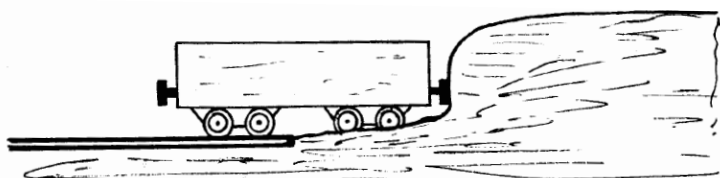
### 1989 Question 13, 1 mark

What is the total kinetic energy of the two trucks after the collision?

### 1989 Question 14, 5 marks

(This is an extended answer question.)

A single truck runs off the end of a straight railway track and stops quickly. It comes to rest as shown below.

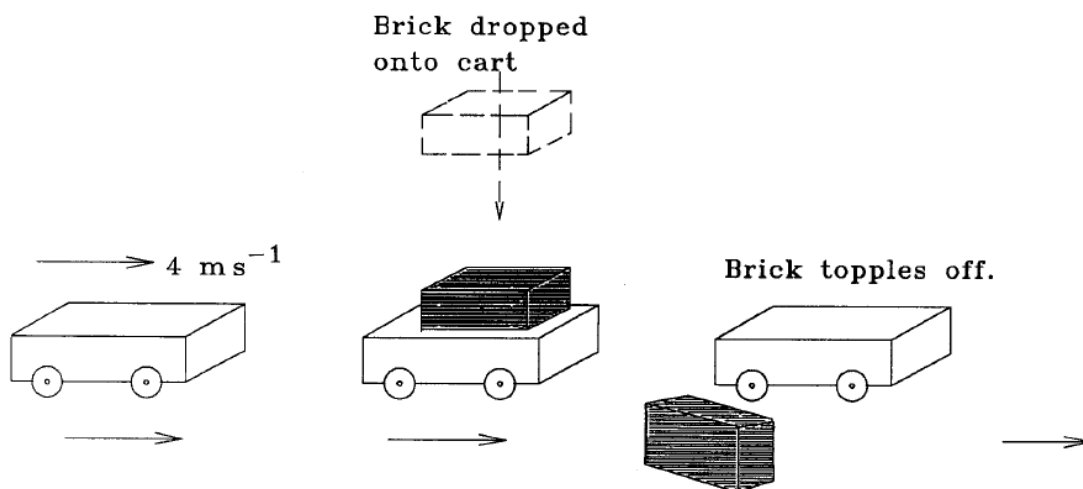


Discuss the forces on the truck and what happens to the momentum and the kinetic energy of the truck. A discussion of impulse should be included.

How would your answer differ if the truck had run onto a hard level surface and taken longer to come to rest?

## Momentum and impulse

Two young children, Dennis and Frank, are playing with some toy carts. Dennis pushes a cart towards Frank with a speed of  $4 \text{ m s}^{-1}$ . As the cart passes him, Frank drops a brick vertically onto it. The brick has a mass equal to that of the cart.



### 1990 Question 9, 1 mark

Just after Frank drops the brick onto it, the speed of the cart will be closest to

- A.  $1 \text{ m s}^{-1}$ .
- B.  $4 \text{ m s}^{-1}$ .
- C.  $2 \text{ m s}^{-1}$ .
- D.  $8 \text{ m s}^{-1}$ .

## Momentum and impulse

After the cart travels a further short distance, the brick topples sideways and falls off.

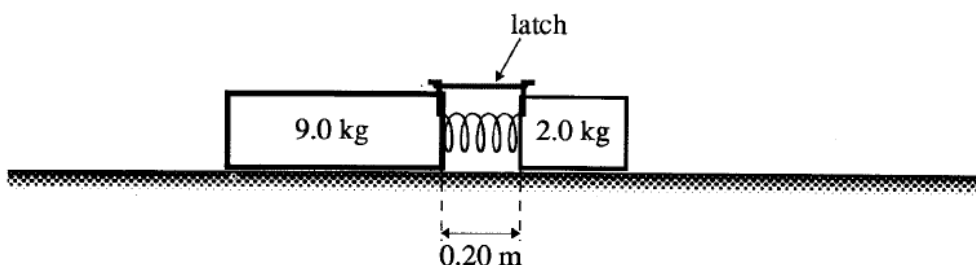
### 1990 Question 10, 1 mark

Just after the brick falls off, the speed of the cart is likely to be close to

- A. the same speed as calculated in Question 9.
- B. about half the speed calculated in Question 9.
- C. about twice the speed calculated in Question 9.
- D. close to zero.

A laboratory demonstration consists of two metal blocks of masses 2.0 kg and 9.0 kg which are coupled together with a latch. Between the blocks is a spring with a spring constant of  $6.0 \times 10^3 \text{ N m}^{-1}$ . Its

normal length is 0.30 m, but in location it has been compressed to 0.20 m.



The blocks are placed at rest on a frictionless surface, and the latch quickly undone, so that the blocks fly apart.

### 1991 Question 15, 1 mark

What is the value of the ratio  $\frac{\text{magnitude of momentum of 2.0 kg block}}{\text{magnitude of momentum of 9.0 kg block}}$

### 1991 Question 16, 1 mark

When the 9.0 kg block has moved 1.8 m, how far has the 2.0 kg block travelled?

Most sports safety helmets are designed to protect the head during impact with the ground following a fall. A helmet usually consists of a liner of polystyrene foam about 2.5 cm thick which is moulded to fit the shape of a

## Momentum and impulse

human head. Some helmets are covered with a hard outer shell of plastic. According to a consumer magazine, the hard shell protects the foam liner but 'does not contribute greatly to the impact absorption of the helmet'.

### 1993 Question 7, 2 marks

The use by the consumer magazine of the term 'impact absorption' is not correct physics terminology. In terms of **one or more** of the physics concepts listed below, describe how a helmet protects a person's head during an impact with the ground.

- force
- impulse
- energy
- momentum
- acceleration

A car is stationary at a stop sign when it is hit directly from behind by a truck of mass 3000 kg which was travelling at a speed of  $9 \text{ m s}^{-1}$  immediately before the collision. The two vehicles lock together and move forward with an initial speed of  $6 \text{ m s}^{-1}$ .

### 1994 Question 6, 1 mark

What is the mass of the car?

Both drivers were wearing correctly adjusted seatbelts at the time of the accident, and the vehicles had strong supporting seat backs with head restraints.

### 1994 Question 7, 1 mark

Which statement (A - D) below best describes the forces arising from the impact, which act on the drivers?

- A.** Each driver felt an increased force due to the seatbelts.
- B.** The driver of the car felt an increased force due to the seatbelt, but the driver of the truck felt an increased force due to the back of the seat.
- C.** Each driver felt an increased force due to the back of the seat.
- D.** The driver of the truck felt an increased force due to the seatbelt, but the driver of the car felt an increased force due to the back of the seat.



## Momentum and impulse

Each driver had a mass of 72.0 kg. During the collision, the driver of the car experienced an average force of 8 000 N.

### **1994 Question 8, 1 mark**

How long did the collision take?

## Momentum and impulse

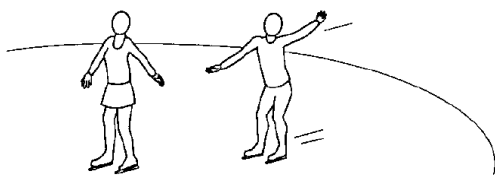
### 1994 Question 9, 1 mark

What was the magnitude of the force experienced by the driver of the truck?

### 1994 Question 10, 2 marks

If the car had been designed with a crumple zone, explain, in correct physics terms, why this might reduce the risk of injury to the driver.

John, of mass 70 kg, and Mary of mass 60 kg, are practising for an ice-skating competition. In the questions below, assume that the ice provides a frictionless surface, and that the skaters do not push against the ice.

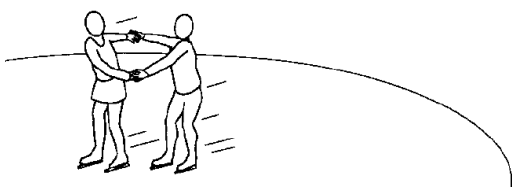


In the figure above, Mary is standing at rest on the ice and John is approaching her with a speed of  $4.0 \text{ m s}^{-1}$ .

### 1995 Question 4, 1 mark

What is the magnitude of John's momentum before he reaches Mary?

In the figure below, John and Mary are moving together in the direction that John was moving before he linked hands with Mary.



### 1995 Question 5, 1 mark

What is the speed of the pair?



## Momentum and impulse

Without pushing or pulling, John and Mary let go of each other.

### 1995 Question 6, 2 marks

Describe the subsequent motions of the two skaters. Your answer should discuss the speed and direction of motion of each skater. You should justify your answer by referring to any relevant physics principles.

A ball of mass 0.100 kg is dropped vertically on to a hard surface, reaching a speed of  $12 \text{ m s}^{-1}$  just before hitting the surface. It rebounds vertically at an initial speed of  $8.0 \text{ m s}^{-1}$ . The contact between ball and surface lasts for a time of 0.0050 s.

### 1996 Question 16, 1 mark

Calculate the magnitude of the change in momentum of the ball during the time of contact.

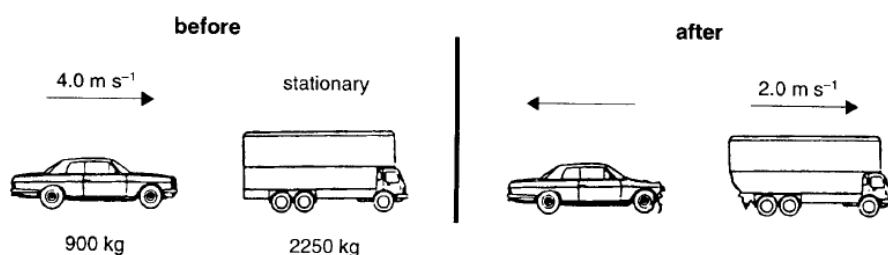
### 1996 Question 17, 1 mark

Calculate the magnitude of the average net force exerted on the ball during the collision.

A car of mass 900 kg, travelling on a horizontal road with a speed of  $4.0 \text{ m s}^{-1}$ , runs into the rear of a stationary truck of mass 2250 kg as shown below. Immediately after the collision the truck moves forward with a speed of  $2.0 \text{ m s}^{-1}$  and the car rebounds in the opposite direction.

In modelling this collision you should assume that

- there is no driving force from either engine during the collision
- no braking takes place during the collision
- the car and truck remain in a straight line.



### 1997 Question 6, 3 marks

What is the speed of the car immediately after the collision?

Momentum and impulse

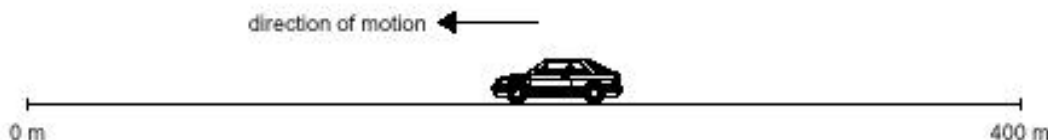
**1997 Question 7, 5 marks**

This was an **inelastic** collision. Explain the meaning of the word inelastic and show, using calculations, that this collision was inelastic.

The “standing 400 m” time for a car is the time that it takes to travel 400 m on a level road, accelerating from rest. The standing 400 m time of a car was 16.0 s.



The test on the car was repeated in the **opposite direction** and the standing 400 m time was 18.0 s.



The momentum of the car at the end of the first 400 m may be represented in magnitude and direction by the vector shown below.



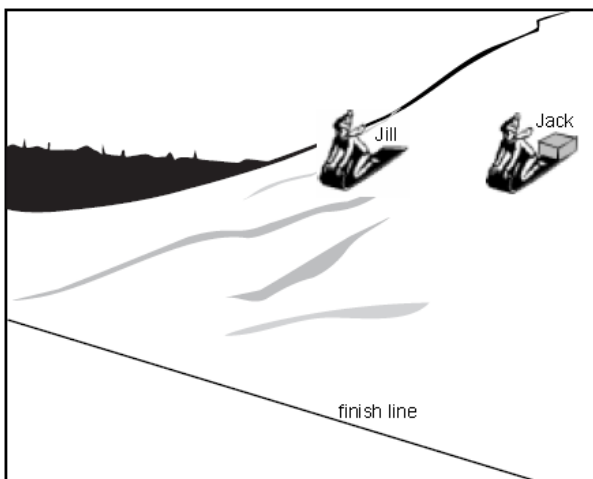
**2000 Question 3, 1 mark**

Which **one** of the vectors (**A – G**) best represents the **momentum change** of the car, between the **end** of the first and the **end** of the second run?

## Momentum and impulse

- A. →
- B. ←
- C. →
- D. ←
- E. →
- F. ←
- G. Zero

Jack and Jill are racing their toboggans down an icy hill. Jack and Jill are of similar mass and are using the same type of toboggan. When Jack is a certain distance from the end of the race they are travelling with the same velocity. Jack is behind Jill and decides that if he is going to win the race, he must lighten his toboggan, so he pushes a box containing their ice-skating gear off the side of his toboggan.

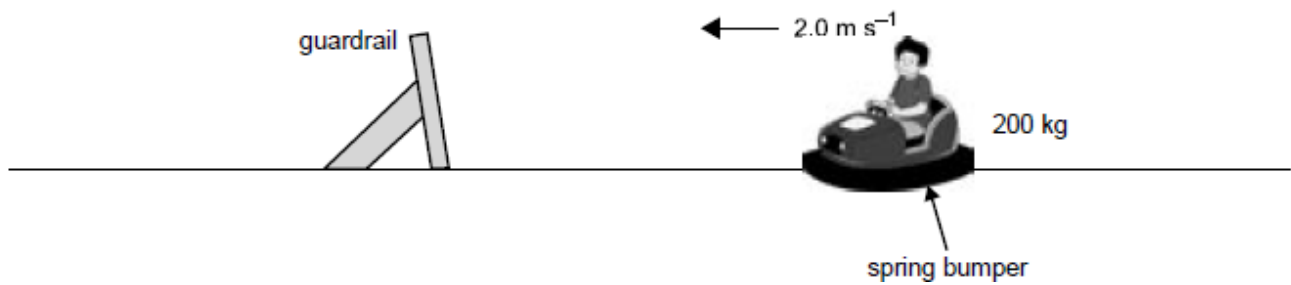


### 2001 Question 11, 4 marks

Explain, giving clear reasons, whether this will be a successful way for Jack to catch up to Jill and help him win the race.

Kim is driving a dodgem car. He is travelling at  $2.0 \text{ m s}^{-1}$  when he hits an oil patch and collides head-on with the guardrail. The dodgem car (shown below) has a spring-loaded bumper. After the collision the dodgem car rebounds directly backwards along the same line at a speed of  $2.0 \text{ m s}^{-1}$ . The spring constant of the bumper is  $3.2 \times 10^5 \text{ N m}^{-1}$  and the mass of Kim and the dodgem car is  $200 \text{ kg}$ .

## Momentum and impulse



The law of conservation of momentum (for an isolated system) is a fundamental law of physics that applies to all collisions.

### 2003 Question 7, 4 marks

Describe how you would show that the collision between the dodgem car and the guardrail satisfies the law of conservation of momentum. In particular, address these three aspects.

Initial momentum of dodgem car

Final momentum of dodgem car

Given the previous answers, explain how momentum is conserved.

A delivery van of mass 1200 kg, travelling south at  $20 \text{ m s}^{-1}$ , collides head-on with a power pole. The impact crushes the crumple zone of the van by 0.60 m bringing the van to rest against the pole.

### 2004 Question 5, 2 marks

Calculate the time for the impact.

### 2004 Question 6, 3 marks

Calculate the initial momentum and final momentum of the van and explain how momentum has been conserved in this collision.

## Momentum and impulse

The following quote was taken from the NASA web site.

*To safely reach the surface of Mars, a spacecraft must decelerate from  $21\,000\text{ km h}^{-1}$  in a matter of minutes and be able to protect its payload as it lands. The Mars Exploration Rovers of 2003 will use a proven airbag system.*

Both physics and non-physics students alike would agree that airbags result in a ‘softer collision’.

### 2004 Question 11, 3 marks

Explain the meaning of the term softer collision in the context of an airbag.

The figure shows a space shuttle docking with the international space station.

Imagine that you are an astronaut floating in space **at rest relative to the international space station**. You watch the space shuttle, of mass  $6000\text{ kg}$ , dock. You observe the shuttle approaching the space station with a speed of  $5.00\text{ m s}^{-1}$ . After docking, the space station’s speed has increased by  $0.098\text{ m s}^{-1}$ .



### 2006 Question 10, 3 marks

Show that the mass of the space station is  $3 \times 10^5\text{ kg}$ .

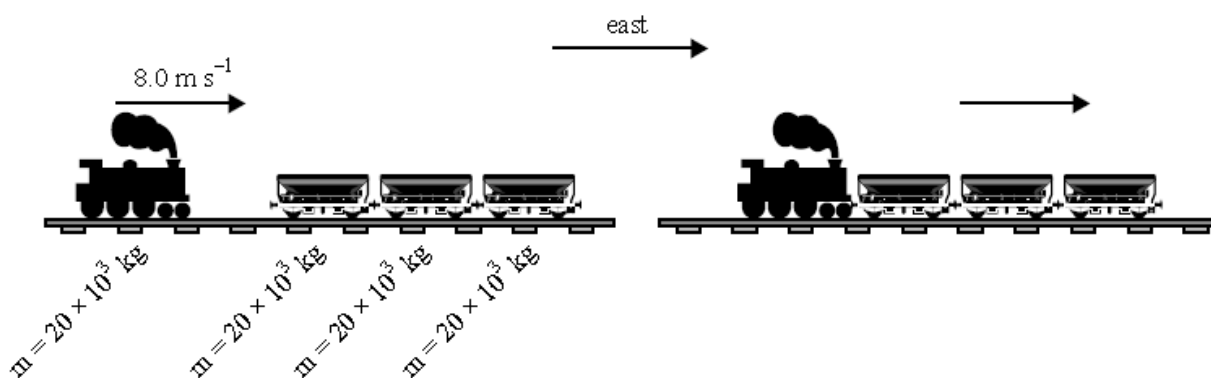


## Momentum and impulse

After first making contact, it takes 20 s for the shuttle to come to rest with the space station.

### 2006 Question 11, 3 marks

A locomotive, of mass  $20 \times 10^3$  kg, moving at  $8.0 \text{ m s}^{-1}$  east, collides with and couples to three trucks, each of mass  $20 \times 10^3$  kg, initially stationary, as shown.



### 2008 Question 8, 2 marks

What is the speed of the coupled locomotive and trucks after the collision?

You must show your working.

### 2008 Question 9, 3 marks

What is the impulse given **to** the locomotive **by** the trucks in the collision (magnitude and direction)? You must show your working.



## Momentum and impulse

### 2008 Question 10, 3 marks

Was this collision elastic or inelastic?

Support your conclusion by appropriate calculation.

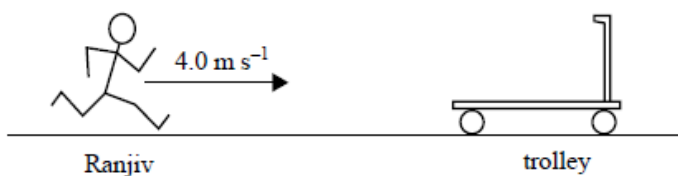
During the collision, the magnitude of the average force exerted by the locomotive on the trucks is  $F_L$  and the magnitude of the average force exerted by the trucks on the locomotive is  $F_T$ .

### 2008 Question 11, 2 marks

Will  $F_L$  be greater, equal to, or less than  $F_T$ ? Explain your answer.

*The following information relates to Questions 1 and 2.*

Ranjiv, who has a mass of 80 kg, is running with a speed of  $4.0 \text{ m s}^{-1}$  as he steps onto a stationary trolley of mass 40 kg as shown below. Ranjiv holds on to the trolley. Ranjiv and the trolley then move forward together in the same direction.



### 2009 Question 1, 2 marks

What is the speed of the trolley as soon as Ranjiv is on board?

### 2009 Question 2, 3 marks

Is this collision between Ranjiv and the trolley elastic or inelastic? Write your answer, **and** justify it with a calculation.

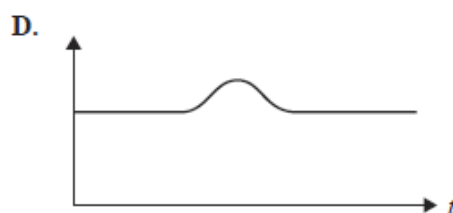
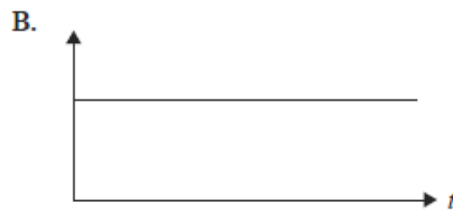
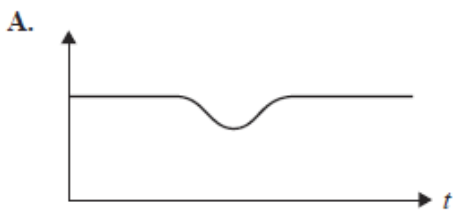
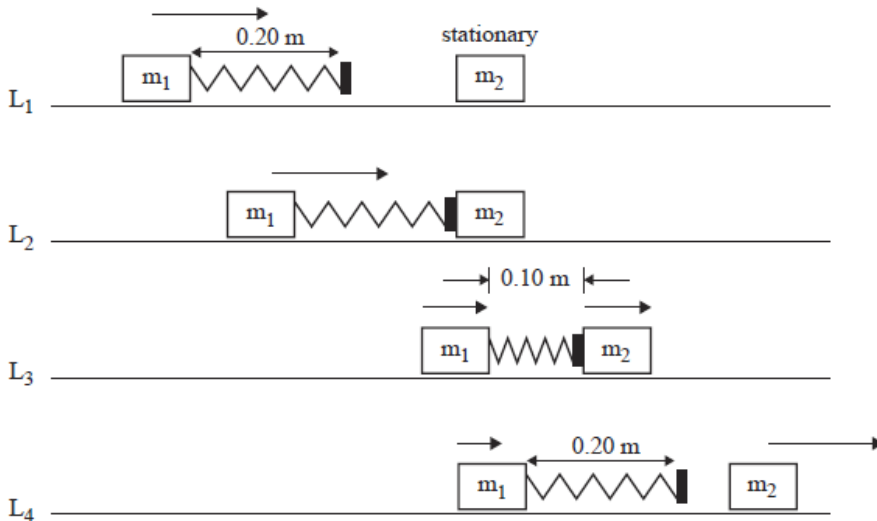
Momentum and impulse

The following information relates to Questions 16–17.

Physics students are conducting a collision experiment using two trolleys,  $m_1$  of mass 0.40 kg and  $m_2$  of mass 0.20 kg.

- Trolley  $m_1$  has a light spring attached to it. When uncompressed, this spring has a length of 0.20 m.
- Trolley  $m_1$  is initially moving to the right. Trolley  $m_2$  is stationary.
- The trolleys collide, compressing the spring to a length of 0.10 m.
- The trolleys then move apart again, and the spring reverts to its original length (0.20 m), and both trolleys move off to the right.
- The collision is elastic.
- The trolleys do not experience any frictional forces.

The situation is shown below.



## Momentum and impulse

### 2010 Question 16, 2 marks

Which graph best shows how the total momentum of the system varies with time before, during and after the collision? Explain your answer.

### 2010 Question 17, 2 marks

If the collision had been inelastic, which graph would best show how the magnitude of the total momentum of the system varies with time before, during and after the collision? Explain your answer.

A 1.2 kg block moves to the right along the frictionless surface and collides elastically with a stationary block of mass 2.4 kg as shown below.



After the elastic collision, the 1.2 kg block moves to the left as shown.

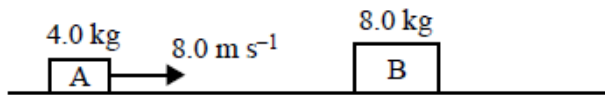


### 2012 Question 2, 3 marks

After the collision, the momentum of the 2.4 kg block is **greater** than the momentum that the 1.2 kg block had before the collision. Explain why the greater momentum of the 2.4 kg block is consistent with the principle of conservation of momentum.

Block A, of mass 4.0 kg, is moving to the right at a speed of  $8.0 \text{ m s}^{-1}$ , as shown below. It collides with a stationary block, B, of mass 8.0 kg, and rebounds to the left. Its speed after the collision is  $2.0 \text{ m s}^{-1}$ .

Momentum and impulse



**2015 Question 1a, 2 marks**

Calculate the speed of block B after the collision.

**2015 Question 1b, 2 marks**

Explain whether the collision is elastic or inelastic. Include some calculations in your answer.

**2015 Question 1c, 3 marks**

What are the magnitude, unit and direction of the impulse by block B on block A?

The engine, of mass 20 tonnes moving to the right at 2.0 m s<sup>-1</sup>, collides with but does not couple with the stationary wagon of mass 10 tonnes. After the collision, the wagon moves off to the right at 2.0 m s<sup>-1</sup>.

**2016 Question 1e, 3 marks**

Calculate the velocity (magnitude and direction) of the engine after the collision. Show your working.

## Momentum and impulse

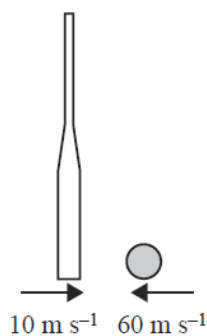
Students are using high-speed photography to analyse the collision between a bat and a ball. The experiment is arranged so that the bat and the ball are both moving horizontally just before and just after the collision, as shown below.

Assume that the bat and the ball are point masses.

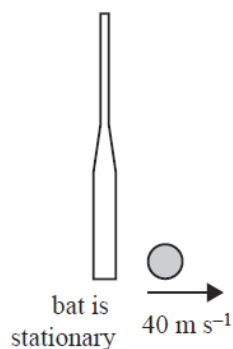
The students record the following measurements.

mass of bat	2.0 kg
mass of ball	0.2 kg
speed of bat immediately before collision	$10 \text{ m s}^{-1}$ (bat is stationary after collision)
speed of ball immediately before collision	$60 \text{ m s}^{-1}$ (towards bat)
speed of ball immediately after collision	$40 \text{ m s}^{-1}$ (away from bat)
time ball is in contact with bat	0.010 s

**Before the collision**



**After the collision**



### 2019 NHT Question 7a, 3 marks

Calculate the magnitude of the impulse given by the bat to the ball. Include an appropriate unit. Show your working.

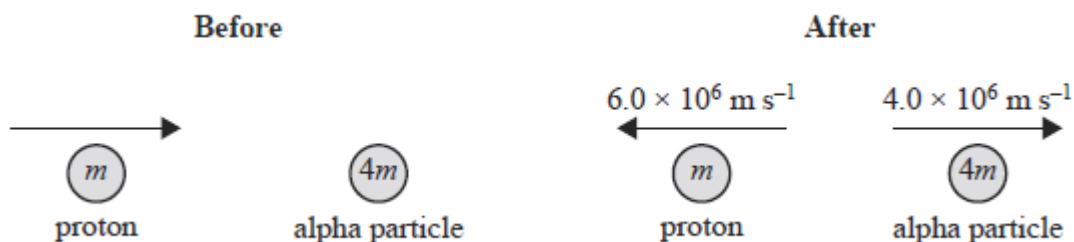
### 2019 NHT Question 7b, 2 marks

Calculate the average force of the bat on the ball during the collision. Show your working.

**2019 NHT Question 7c, 2 marks**

Use calculations to determine whether the collision between the bat and the ball is elastic or inelastic. Show your working.

A proton in an accelerator detector collides head-on with a stationary alpha particle, as shown below. After the collision, the alpha particle travels at a speed of  $4.0 \times 10^6 \text{ m s}^{-1}$ . The proton rebounds at  $6.0 \times 10^6 \text{ m s}^{-1}$ .



**2019 Question 9, 3 marks**

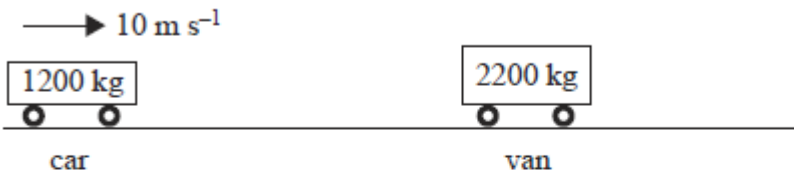
Find the speed of the proton before the collision, modelling the mass of the alpha particle,  $4m$ , to be equal to four times the mass of the proton,  $m$ . Show your working. Ignore relativistic effects.

Jacinda designs a computer simulation program as part of her practical investigation into the physics of vehicle collisions. She simulates colliding a car of mass 1200 kg, moving at  $10 \text{ m s}^{-1}$ , into a stationary van of mass 2200 kg. After the collision, the van moves to the right at  $6.5 \text{ m s}^{-1}$ . This situation is shown below.

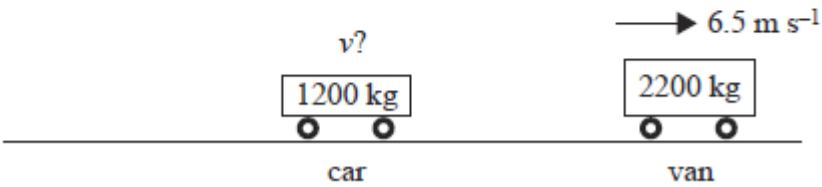


## Momentum and impulse

### Before collision



### After collision



### 2020 Question 10a, 4 marks

Calculate the speed of the car after the collision and indicate the direction it would be travelling in.

Show your working.

### 2020 Question 10b, 3 marks

Explain, using appropriate physics, why this collision represents an example of either an elastic or an inelastic collision.

### 2020 Question 10c i, 3 marks

The collision between the car and the van takes 40 ms.

Calculate the magnitude and indicate the direction of the average force on the van by the car.

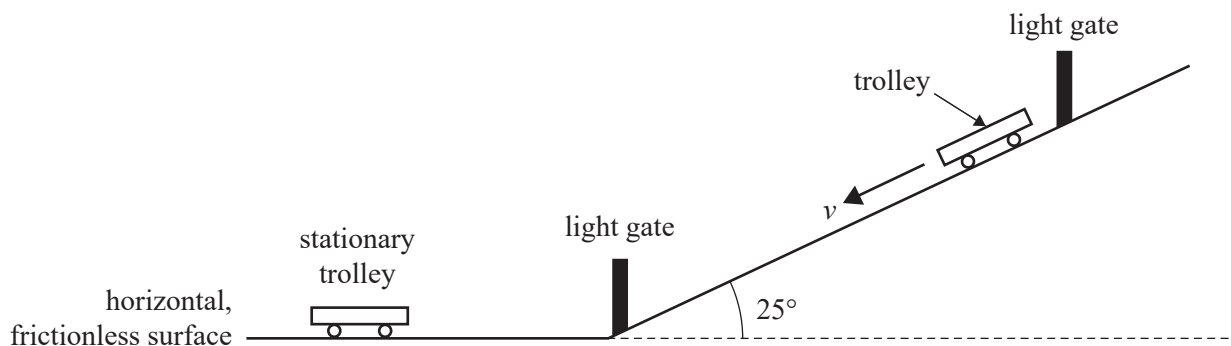
Momentum and impulse

**2020 Question 10c ii, 2 marks**

Calculate the magnitude and indicate the direction of the average force on the car by the van.

**Question 7** (10 marks)

Kym and Kelly are experimenting with trolleys on a ramp inclined at  $25^\circ$ , as shown in Figure 7. They release a trolley with a mass of  $2.0\text{ kg}$  from the top of the ramp. The trolley moves down the ramp, through two light gates and onto a horizontal, frictionless surface. Kym and Kelly calculate the acceleration of the trolley to be  $3.2\text{ m s}^{-2}$  using the information from the light gates.



**Figure 7**

- a. i.** Show that the component of the gravitational force of the trolley down the slope is  $8.3\text{ N}$ .  
Use  $g = 9.8\text{ m s}^{-2}$ . 2 marks

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- ii.** Assume that on the ramp there is a constant frictional force acting on the trolley and opposing its motion.  
Calculate the magnitude of the constant frictional force acting on the trolley. 2 marks

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N

**b.** When it reaches the bottom of the ramp, the trolley travels along the horizontal, frictionless surface at a speed of  $4.0 \text{ m s}^{-1}$  until it collides with a stationary identical trolley. The two trolleys stick together and continue in the same direction as the first trolley.

- i.** Calculate the speed of the two trolleys after the collision. Show your working and clearly state the physics principle that you have used. 3 marks

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$\text{m s}^{-1}$
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- ii.** Determine, with calculations, whether this collision is an elastic or inelastic collision. Show your working. 3 marks

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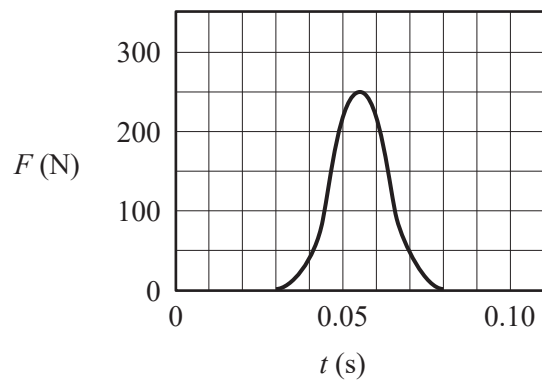
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**Question 4**

The diagram below shows the force versus time graph of the force on a tennis ball when it is hit by a tennis racquet. The tennis ball is stationary when the tennis racquet first comes into contact with the ball.



Which one of the following is closest to the impulse experienced by the tennis ball as it is hit by the tennis racquet?

- A. 0.50 N s
- B. 5.0 N s
- C. 10 N s
- D. 50 N s